



*Parallel Cooperative
Optimization Research
Group*

Reusable design of single solution-based metaheuristics

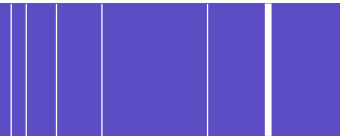


Laboratoire d'Informatique
Fondamentale de Lille



The main steps to build a Solution-based metaheuristic

- Always:
 - The neighborhood/the moves and some operators to manages it/them,
 - The way to initialize the starting condition.
- Specialist:
 - Neighborhood selection strategy,
 - Cooling schedule,
 - Tabu list, ...
 - The continuation criterion.



Framework and tutorial application

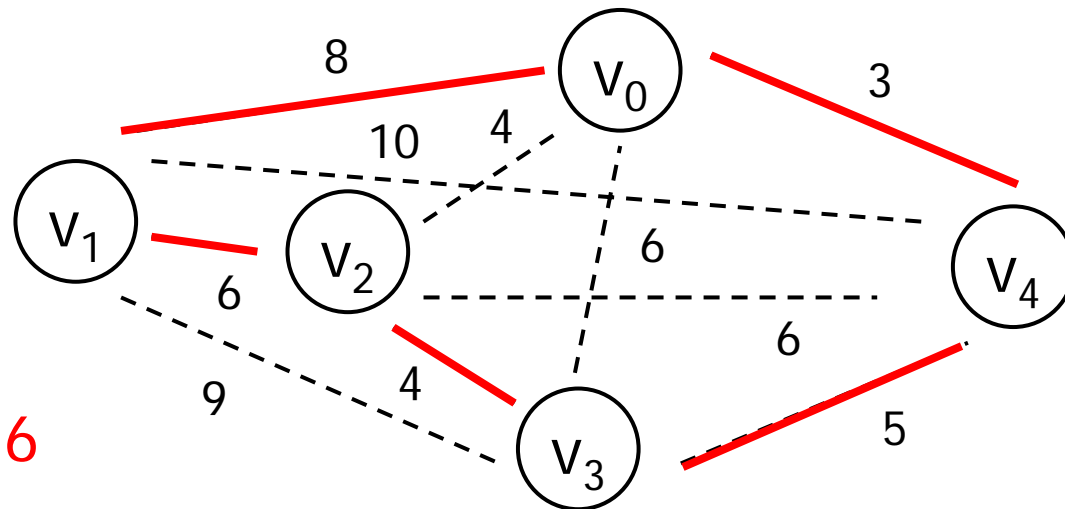
- A framework for the design of Local Searches (Hill Climbing, Simulated Annealing and Tabu Search):
 - Moving Objects (MO).
- Tutorial application:
 - The Traveling Salesman Problem (TSP).

Moving Objects (MO)

- A framework that extends the EO library in order to design solution-based meta-heuristics.
- Design/development team:
 - S. Cahon, N. Melab and E-G Talbi (OPAC-LIFL).

Application to the **T**raveling **S**alesman **P**roblem (**TSP**)

- “Given a collection of N cities and the distance between each pair of them, the **TSP** aims at finding the shortest route visiting all of the cities”.
- Symmetric TSP.
- Example:



Length: 26

Common features

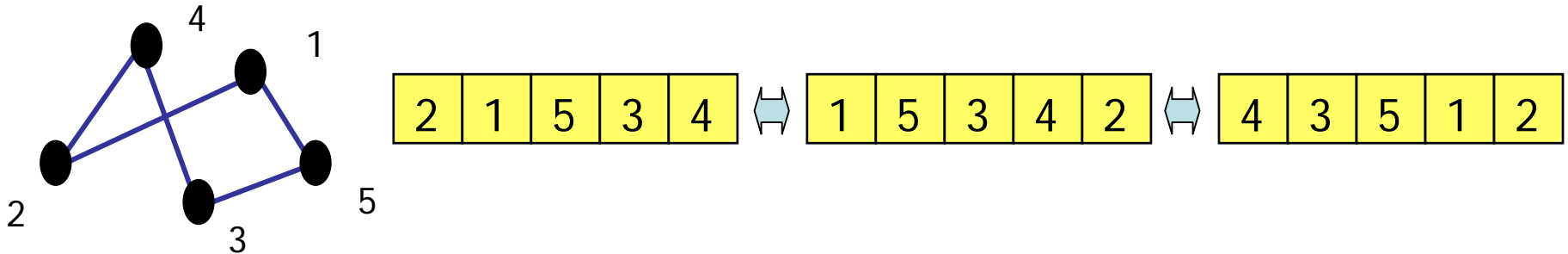


Designing the neighborhood

- It is strongly dependant of the representation of the solution !
- The nature of the landscape depends on it.
- Issues:
 - Moves that imply minor changes are preferred,
 - Fitness delta should be easily and efficiently computed,
 - Analysis of complexity (i.e. size of the neighborhood).

Application to the TSP

- Reminding the chosen coding.
→ Ordered sequence of visited vertices.



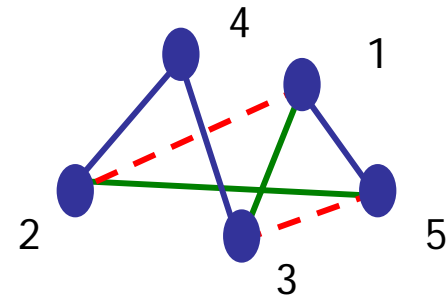
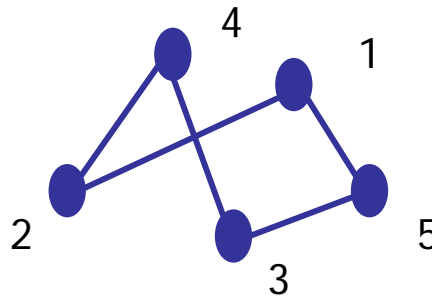
- Some relevant moves:
 - Two-opt, City-swap, LK, etc...

Two-Opt

- Two points within the string are selected and the segment between them is inverted. This operator put in two new edges in the tour.

| | | | | |
|---|---|---|---|---|
| 2 | 1 | 5 | 3 | 4 |
|---|---|---|---|---|

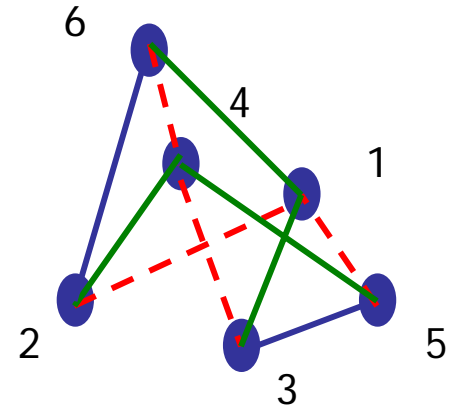
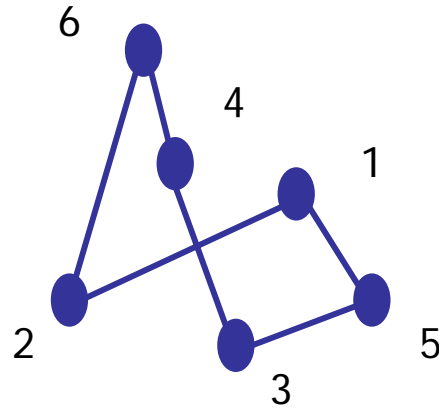
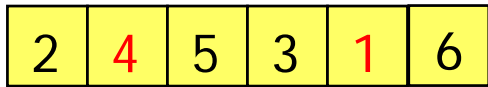
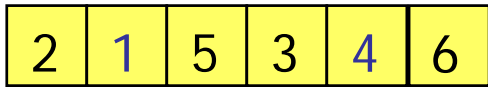
| | | | | |
|---|---|---|---|---|
| 2 | 5 | 1 | 3 | 4 |
|---|---|---|---|---|



$$\Delta = -d(2,1) - d(5,3) + d(2,5) + d(1,3)$$

City-Swap

- The values contained in two positions are exchanged, thus introducing four new edges in the string.



$$\text{Delta} = -d(2,1) - d(1,5) - d(3,4) - d(4,6) \\ + d(2,4) + d(4,5) + d(3,1) + d(1,6)$$

It is known less efficient than City-swap for many instances !

Strategies for the starting solution (to improve)

- Two main used cases in practice:
 - A randomly generated initial solution,
 - A solution built by another metaheuristic (greedy algorithm, genetic algorithm, ...).

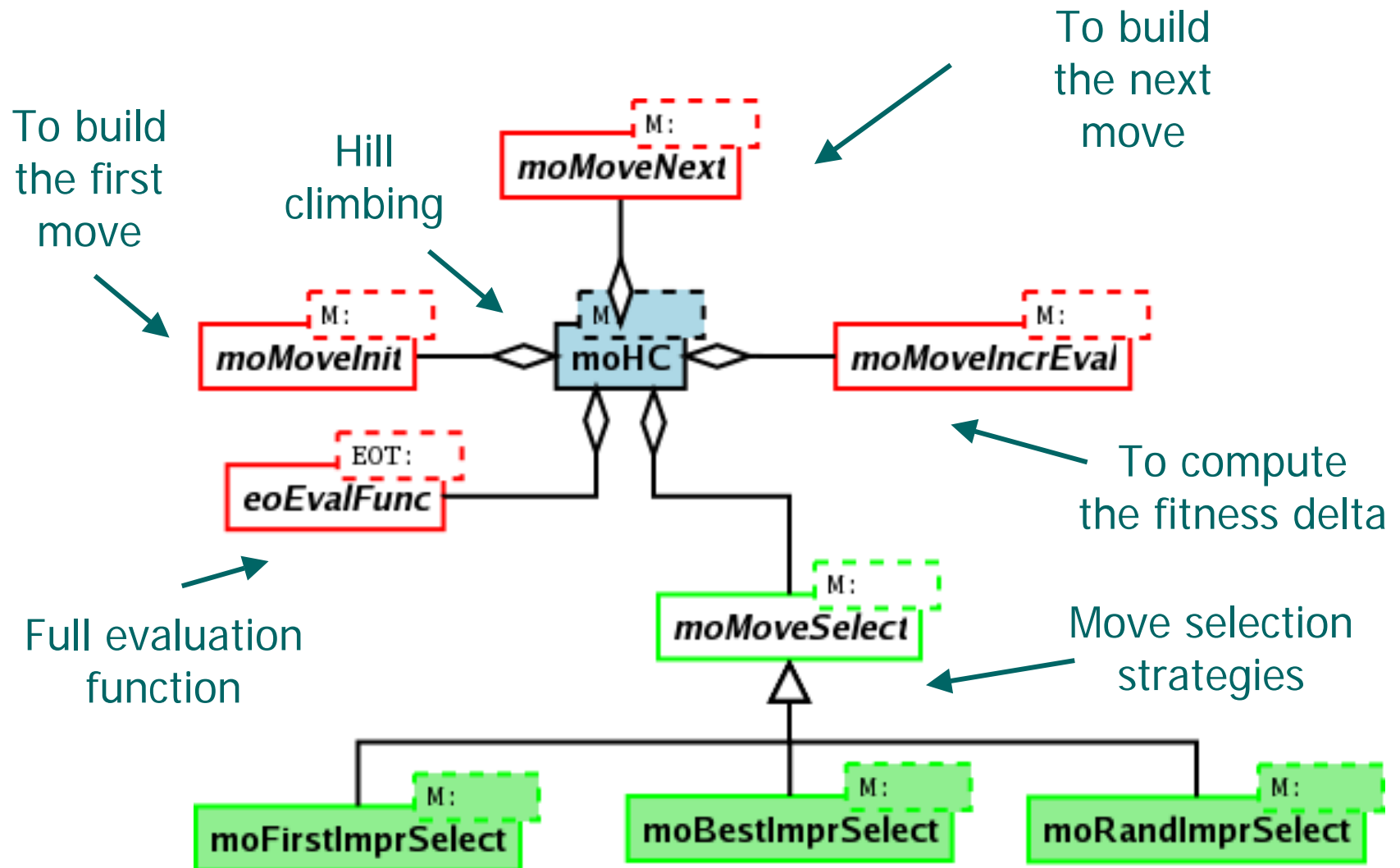
Hill Climbing



How to build a Hill Climbing ?

- Design a **move operator**, its features.
- Design/implement the operator to build the **first move** (and implicitly the first neighboring candidate).
- Design/implement the operator to update a given move to its **successor**.
- Design/implement the **incremental evaluation function**.
- Chose the **neighbour selection strategy**.
- **No continuation criterion** (stopping as a local optima is reached).

Core classes

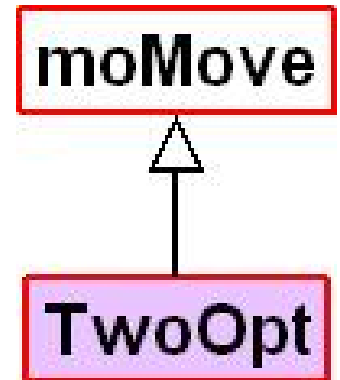


The Two-Opt move

- A Two-opt move is a couple of positions in the sequence of visited nodes.

```
class TwoOpt : public moMove <Route>, public std :: pair <unsigned, unsigned> {  
public :  
    void operator () (Route & __route);  
};
```

← To be implemented



The Two-Opt move initializer

- It initializes both positions to zero !

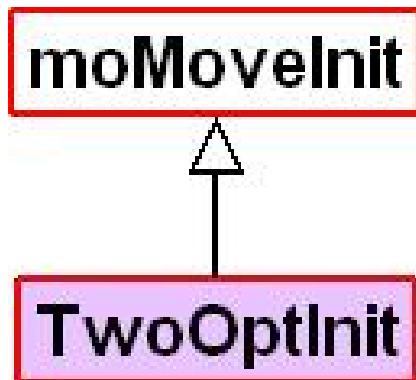
```
class TwoOptInit : public moMoveInit <TwoOpt> {
```

```
public :
```

```
    void operator () (TwoOpt & __move, const Route & __route) ;  
};
```



To be implemented



The Two-Opt move updater

- It increments the second position if possible. Else, it increments the first position, and reinitializes the second position.

```
class TwoOptNext : public moMoveNext <TwoOpt> {
```

```
public :
```

```
    bool operator () (TwoOpt & __move, const Route & __route) ;  
};
```

Succeeding in building
the next move

To be implemented

moMoveNext

TwoOptNext

The Two-Opt move incremental evaluation function

- It computes the new length from the costs of the added/removed edges.

```
class TwoOptIncrEval : public moMoveIncrEval <TwoOpt> {
```

```
public :
```

```
int operator () (const TwoOpt & __move, const Route & __route) ;  
};
```

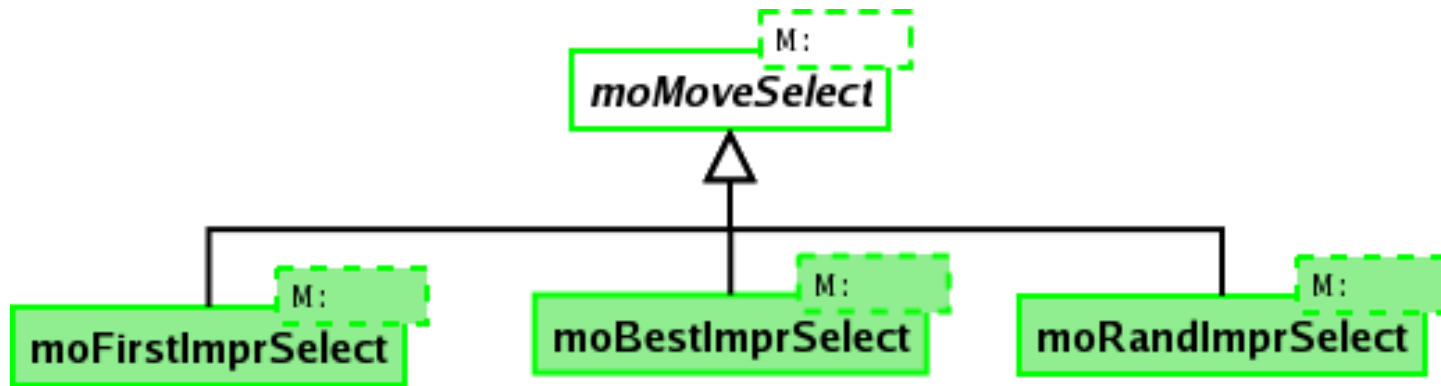
New length

To be implemented

moMoveIncrEval

TwoOptIncrEval

Neighbour selection strategy



- Deterministic/full: choosing the **best neighbor** (i.e. that improves the most the cost function).
- Deterministic/partial: choosing **the first processed neighbour that is better** than the current solution.
- Stochastic/full: processing the whole neighborhood and applying **a random better one**.

Implementation of a Hill Climbing

```
Route route; /* One solution */
RouteInit route_init; /* Its builds random routes */
route_init (route); /* Building a random starting solution */

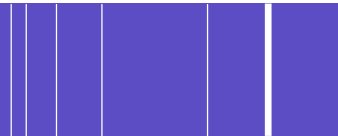
RouteEval full_route_eval; /* Full route evaluator */

TwoOptInit two_opt_init; /* Initializing the first couple of edges to swap */
TwoOptNext two_opt_next; /* Updating a movement */
TwoOptIncrEval two_opt_incr_eval; /* Efficiently evaluating a given neighbor */

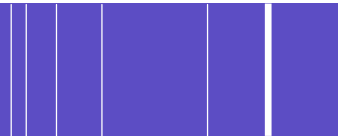
moBestImprSelect <TwoOpt> two_opt_move_select; /* Movement selection
                                                    strategy (elitist) */

/* Building the Hill Climbing from those components */
moHC <TwoOpt> hill_climbing (two_opt_init, two_opt_next, two_opt_incr_eval,
two_opt_move_select, full_route_eval);

/* It applies the HC to the solution */
hill_climbing (route);
```



Simulated Annealing



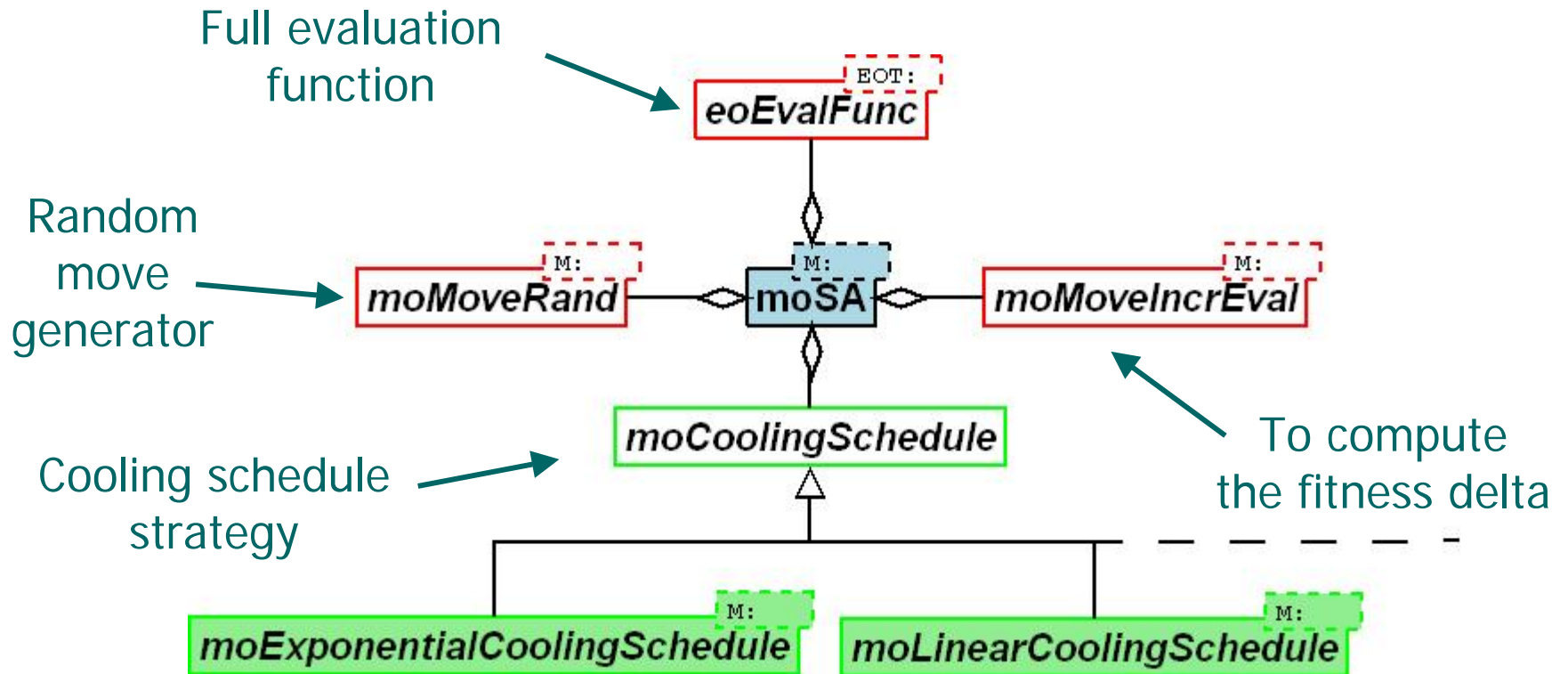
How to build a Simulated Annealing ?

Could be reused from Hill Climbing

- Design a move operator, its features
- Design/implement the operator to build a random candidate move
- Design/implement the incremental evaluation function
- Chose the cooling schedule strategy

Independent of the tackled problem

Core classes



The Two-Opt random move generator

- It randomly determines a couple of random positions !

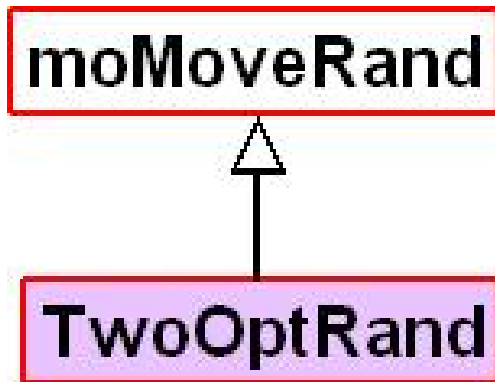
```
class TwoOptRand : public moMoveRand<TwoOpt> {
```

```
public :
```

```
void operator () (TwoOpt & __move, const Route & __route) ;  
};
```

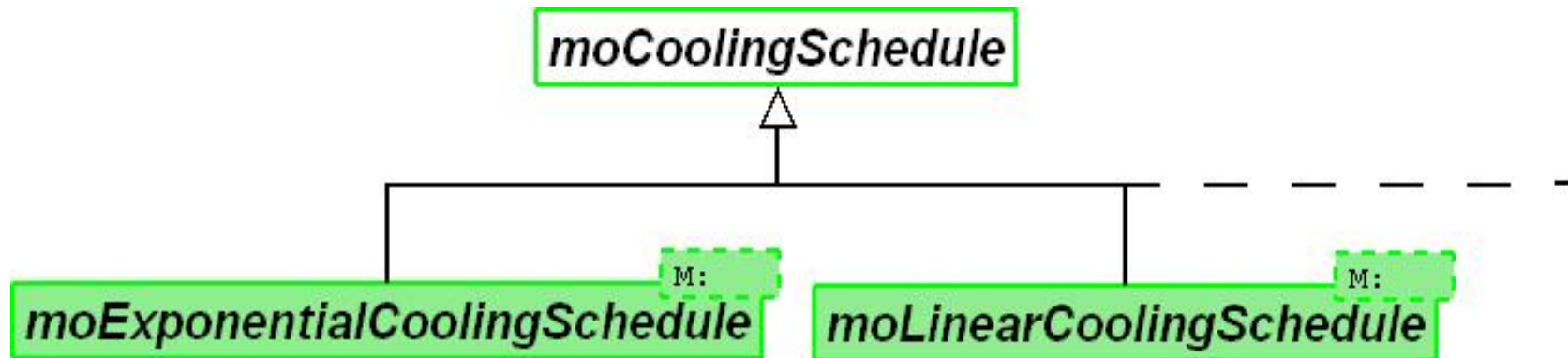


To be implemented



Cooling Schedule

- Two (basic) strategies are already implemented: linear and exponential:
 - **Linear** $\Leftrightarrow temp = temp - x$.
 - **Exponential** $\Leftrightarrow temp = temp * x$.



Implementation of Simulated Annealing

```
RouteInit route_init; /* Its builds random routes */  
route_init (route); /* Building a random starting solution */
```

```
RouteEval full_route_eval; /* Full route evaluator */
```

```
TwoOptRand two_opt_rand; /* It builds random candidate movements */  
TwoOptIncrEval two_opt_incr_eval; /* Efficiently evaluating a given neighbor */
```

```
moExponentialCoolingSchedule cool_scheme (0.99, 1); /*Cooling schedule and  
associated parameters */
```

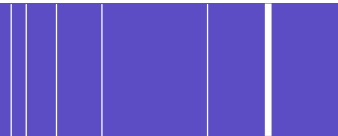
Factor and threshold

```
/* Building the Simulated Annealing from those components */  
moSA <TwoOpt> simulated_annealing (two_opt_init, two_opt_incr_eval, 100,  
100, cool_scheme, full_route_eval);
```

```
/* It applies the SA to the solution */  
simulated_annealing (route);
```

Init. Temp and number of
iter. At any step

Tabu Search



How to design a Tabu Search

- Design a move operator, its features
- Design/implement the operator to build the first move (and implicitly the first neighboring candidate)
- Design/implement the operator to update a given move to its successor
- Design/implement the incremental evaluation function

Could be reused from Hill Climbing

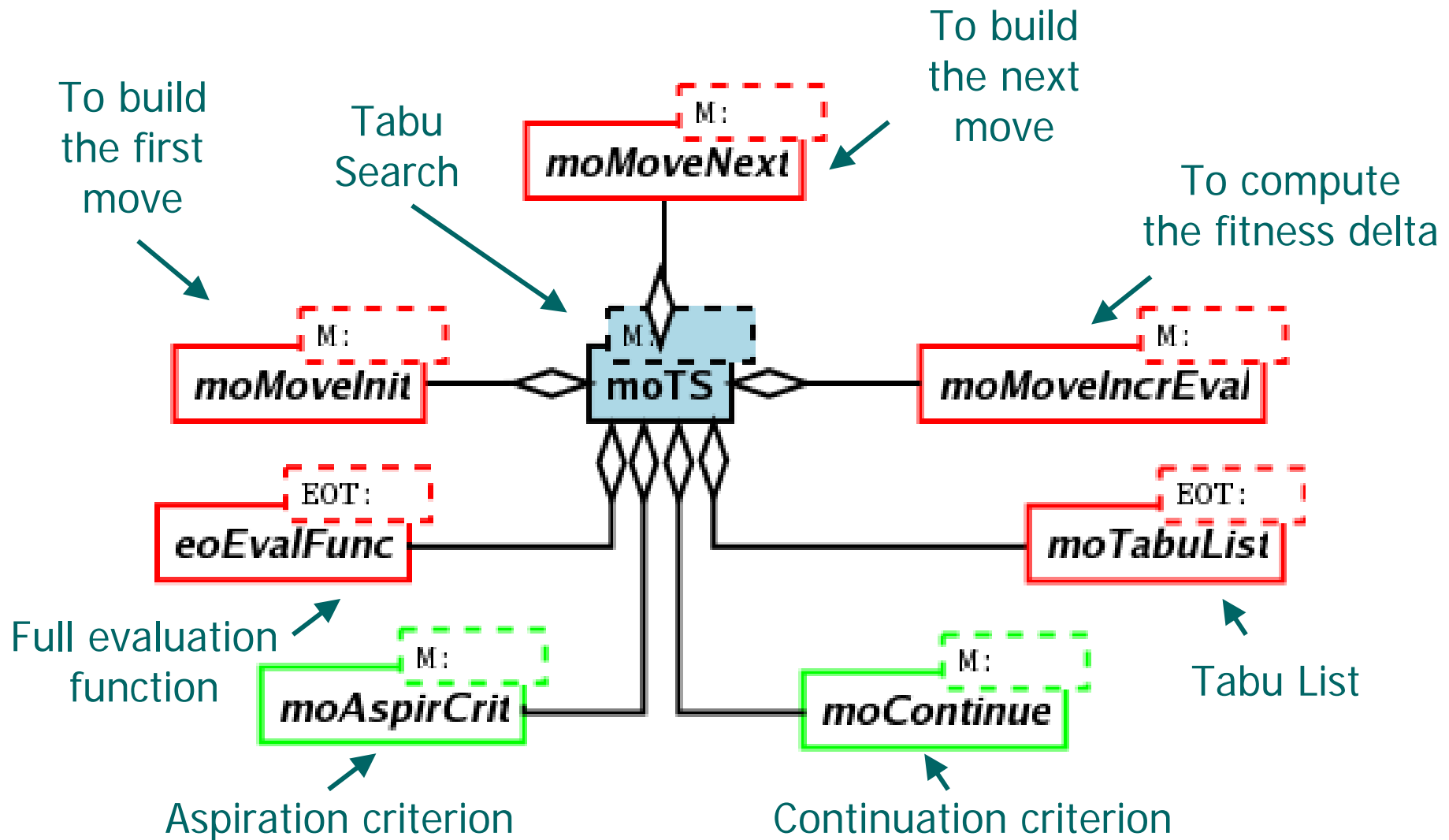
- Design/implement the Tabu List

- Choose the aspiration criterion

- Choose the continuation criterion

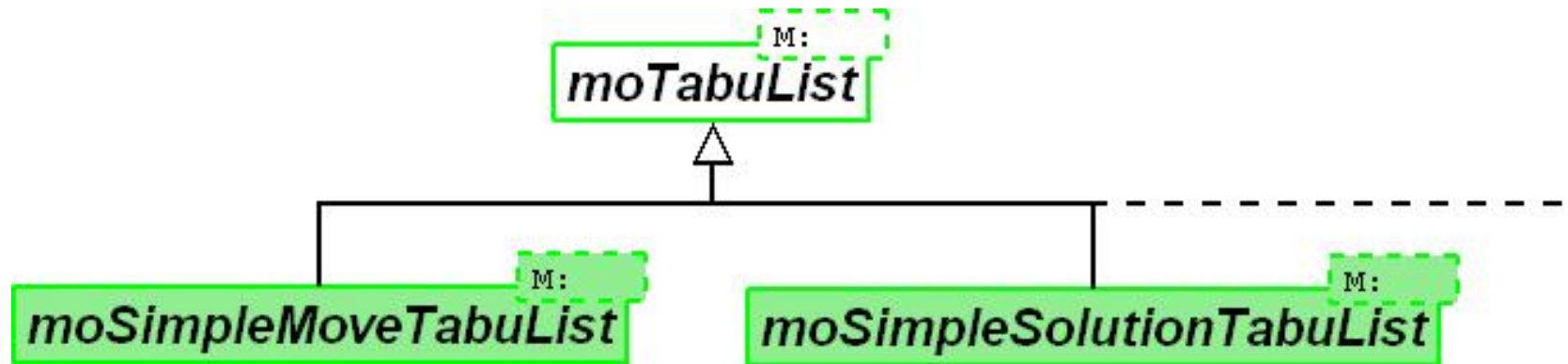
Independent
of the tackled
problem

Core classes



Designing/implementing the Tabu List (1/2)

- Predefined structures:
 - List of tabu solutions or tabu moves storing the tenure (short term memory).



Designing/implementing the Tabu List (2/2)

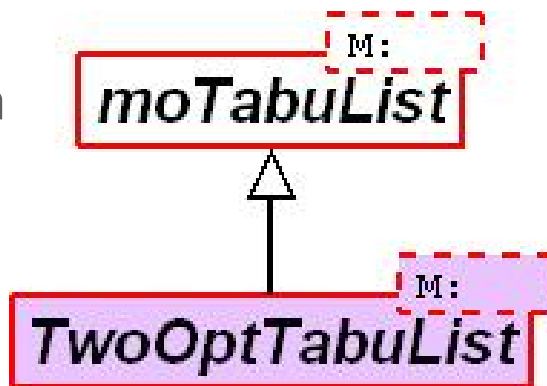
- Regards the two-opt in TSP, it is preferred to build another efficient and more adapted structure.

```
class TwoOptTabuList : public moTabuList <TwoOpt> {
```

```
public :
```

```
    int operator () (const TwoOpt & __move, const Route & __route) ;  
};
```

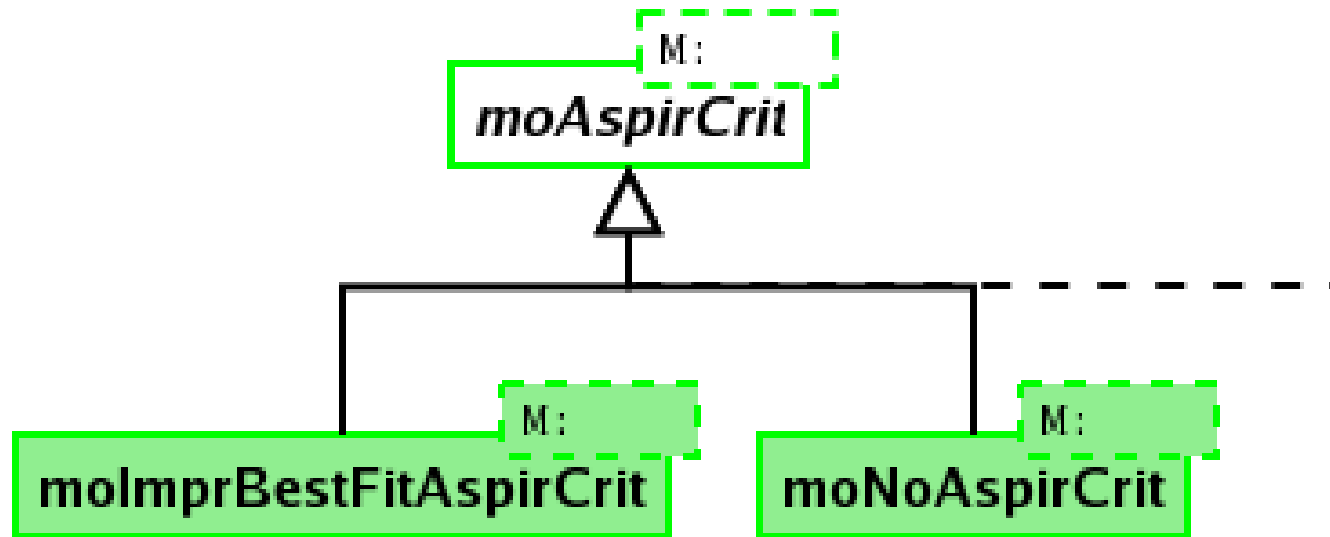
New length



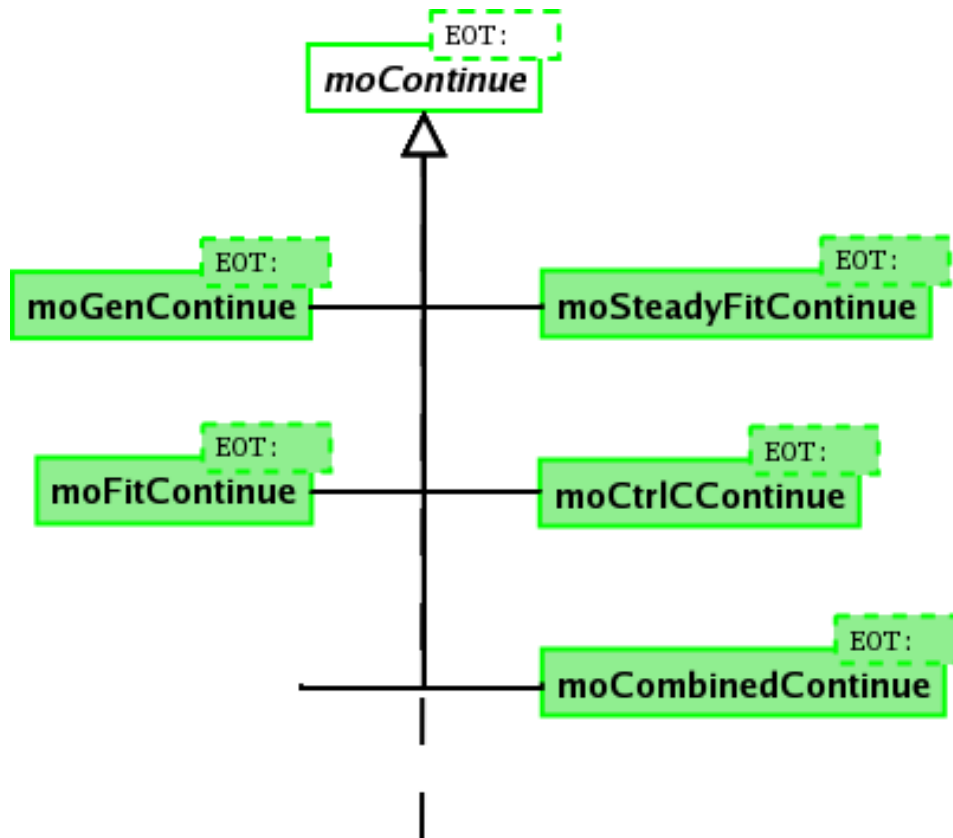
To be implemented

Choosing an aspiration criterion (1/2)

- (Basic) implemented strategies
 - No aspiration criterion,
 - A tabu move builds a new solution that updates the best solution found during the search.



Choosing a continuation criterion (2/2)



- Same strategies as those provided in the design of an Evolutionary Algorithm
 - An optimum is reached,
 - A given total number of iterations,
 - A given number of gen. without improvement,
 - ...

Implementing a Tabu Search

```
Route route; /* One solution */
RouteInit route_init; /* Its builds random routes */
route_init (route); /* Building a random starting solution */

RouteEval full_route_eval; /* Full route evaluator */

TwoOptInit two_opt_init; /* Initializing the first couple of edges to swap */
TwoOptNext two_opt_next; /* Updating a movement */
TwoOptIncrEval two_opt_incr_eval; /* Efficiently evaluating a given neighbor */

moNoAspirCrit <TwoOpt> two_opt_aspir_crit; /* Aspiration criterion */
TwoOptTabuList <TwoOpt> two_opt_tabu_list; /* Tabu List */

moGenContinue <TwoOpt> cont (10000); /* A fixed number of iter. */

/* Building the Tabu Search from those components */
moTS <TwoOpt> tabu_search (two_opt_init, two_opt_next, two_opt_incr_eval,
two_opt_aspir_crit, two_opt_tabu_list, cont, full_route_eval);

/* It applies the TS to the solution */
tabu_search (route);
```